

This question paper contains 4 printed pages.

B.C.A. (Pt. II)

232

Disc. Math.

B.C.A. (PART II) EXAMINATION - 2018
(FACULTY OF SCIENCE)
(Three - Year Scheme of 10+2+3 Pattern)
Paper 232
DISCRETE MATHEMATICS

Time allowed : Three Hours

Maximum Marks : 100

- Part I. (Very short answer) consists of 10 questions of 2 marks each. Maximum limit for each question is up to 40 words.
- Part II: (Short answer) consists of 5 questions of 4 marks each. Maximum limit for each question is up to 80 words.
- Part III - (Long answer) consists of 5 questions of 12 marks each with internal choice.

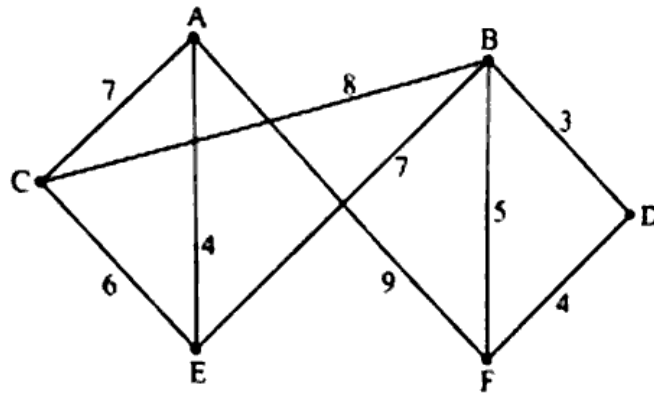
PART - I

1. Very Short Answer Type Questions

- Convert the decimal number $(156)_{10}$ into binary form.
- Compute the sum $(11011)_2 + (10011)_2$ into decimal form.
- Define union of two sets.
- Define equivalence relation.
- By using truth table, for two statements p and q in usual notations show that $p \vee (p \wedge q) = p$.
- For all elements 'a' of Boolean Algebra show that $a + 1 = 1$.
- Define degree of a vertex in graphs.
- What do you mean by proper colouring and chromatic number of a graph.
- Define rooted and binary trees.
- Define minimal spanning tree.

PART - II

- Find the coefficient of x^4 in the expression $\frac{1}{(x-3)(x-2)^2}$.
- If A and B are any two sets, then prove that : $(A \cup B)' = A' \cap B'$.
- For any two statements p and q show that $(p \wedge q) \Rightarrow (p \vee q)$ is a tautology.
- If in a graph $G = (V, E)$ there are n vertices and e edges then prove that in the complementary graph \bar{G} the number of vertices will be $\frac{n(n-1)}{2} - e$.
- Find the minimal spanning tree by Krushal's algorithm in the following graph:



PART - III

7. (a) Compute $(38)_{10} + (69)_{10} = ()_2$
 (b) Compute $(11011)_2 - (10011)_2 = ()_2$
 (c) Use mathematical induction to prove that the sum of the first n odd positive integers is n^2 .
 (d) Using generating function find the solution of the recurrence relation.
 $a_r - 5a_{r-1} + 6a_{r-2} = 0, r \geq 2, a_0 = 6, a_1 = 30.$

OR

- (a) Compute $(11001)_2 - (11101)_2 = ()_2$
 (b) Compute $(46)_n - (146)_n = ()_7$
 (c) Using mathematical induction method prove that:
 $1^2 + 2^2 + 3^2 + \dots + n^2 = \frac{n(n+1)(2n+1)}{6}, (n \geq 1)$
 (d) Find the solution of the recurrence relation:
 $a_r - 3a_{r-1} + 2^r, r \geq 1, a_0 = 1.$
8. (a) If A, B, C and D are any four sets, then prove that $(A \times B) \cap (C \times D) = (A \cap C) \times (B \cap D).$
 (b) If $f: Q \rightarrow Q, f(x) = 2x$ and $g: Q \rightarrow Q, g(x) = x + 2$ then verify $(g \circ f)^{-1} = f^{-1} \circ g^{-1}.$

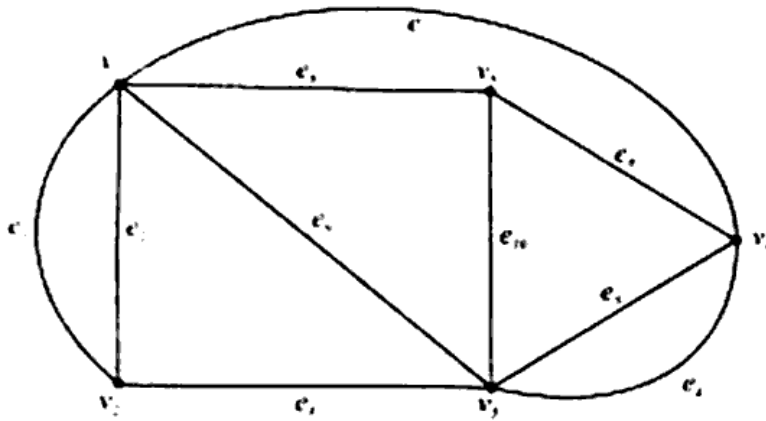
OR

- (c) For any three sets A, B and C, show that $A - (B \cup C) = (A - B) \cap (A - C).$
 (f) On the set of real numbers, a binary operation $*$ is defined as
 $a * b = a - b + ab,$ show that this binary operation is commutative and associative.
9. (a) If p and q are two statements, then by preparing truth table show that the compound statements $p \Leftrightarrow q$ and $(p \wedge q) \vee (\sim p \wedge \sim q)$ are logically equivalent. <https://www.uoronline.com>
 (b) What are the different methods of proving theorems. Prove that $\sqrt{2}$ is irrational number by giving a proof by contradiction.

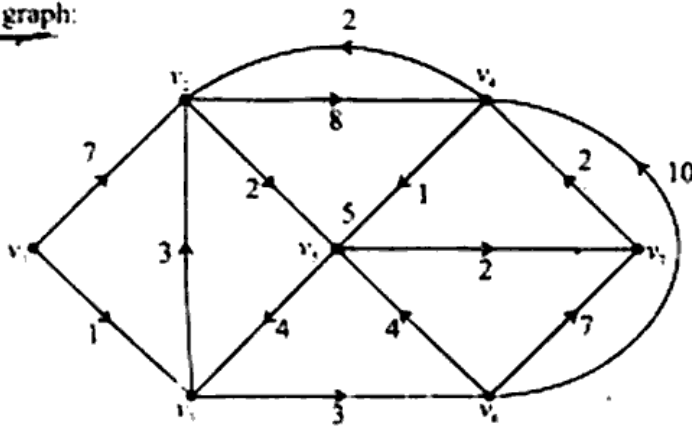
OR

- (a) Prove that no Boolean algebra can have exactly three distinct elements.
 (b) If a, b, c are any three arbitrary elements of the Boolean algebra $(B, +, \dots)$ such that $a + b = a + c$ and $a \cdot b = a \cdot c$ then prove that $b = c.$

10. (a) Find the incident matrix and adjacency matrix of the following graph:



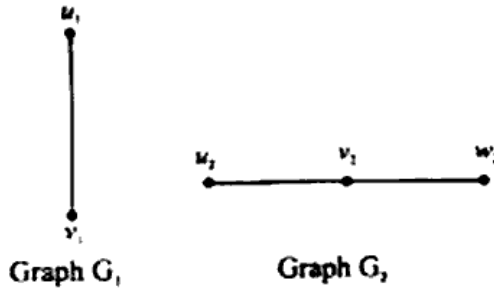
(b) Find the shortest path and shortest distance from the vertices v_1 to v_6 in the following weighted graph:



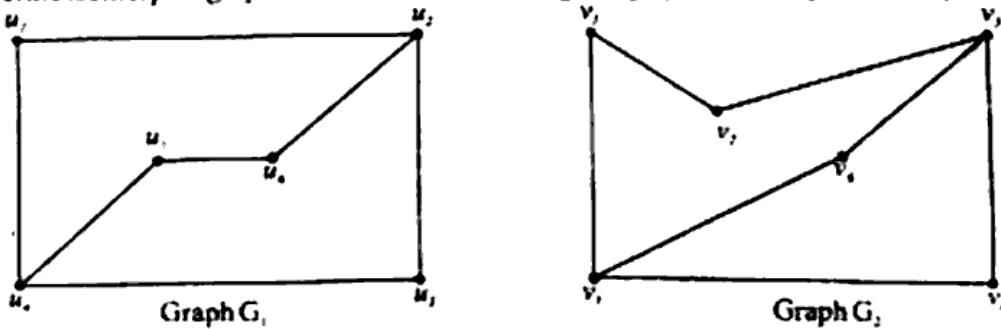
8, 11
7, 1

OR

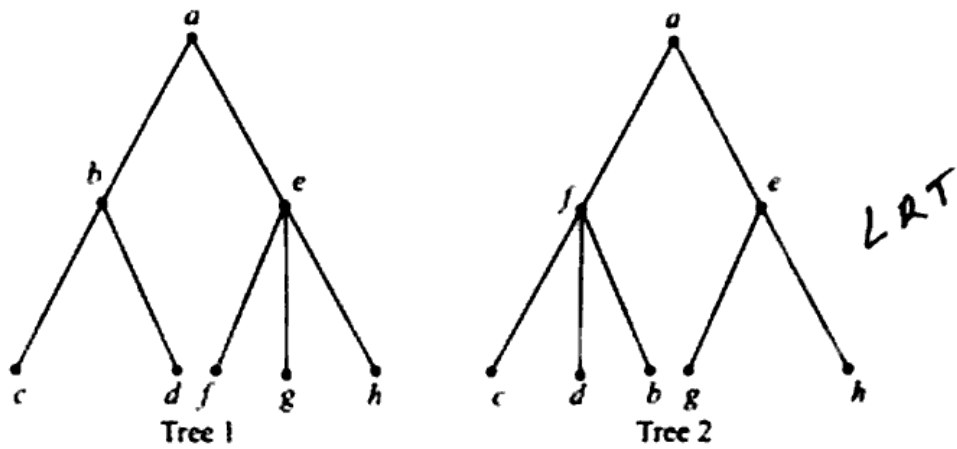
(a) Find product $G_1 \times G_2$ and composition $G_1[G_2]$ of the following two graphs G_1 and G_2 . Also write number of vertices and edges in the resulting graphs:



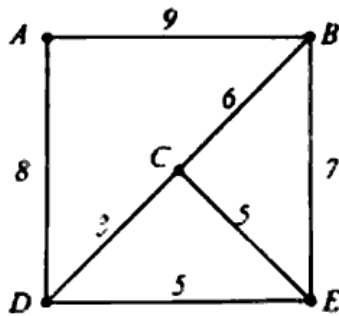
(b) Define isomorphic graphs. Show that the following two graphs G_1 and G_2 are isomorphic:



11. (a) What are the commonly used methods for tree traversal. Show that postorder traversals of the following two ordered rooted trees produce the same list of vertices:



- (b) Find the minimal spanning tree from the following graph by Prim's method:



OR

- (a) Define the following with example:

- (i) Leaf of a tree
- (ii) Tree traversal
- (iii) Path length of a binary tree

- (b) What is the ordered rooted tree that represents the expression $((a+b) \uparrow 2) + ((a-4) / 3)$. What is the value of the prefix expression $+ - * 2 3 5 / \uparrow 2 3 4$?